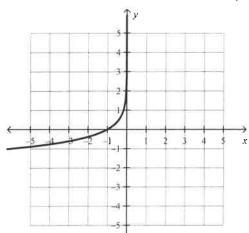
Pre-Calculus 12 Chapter 8 Review

Multiple Choice

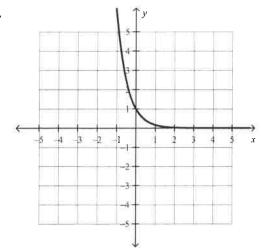
Identify the choice that best completes the statement or answers the question.

1. Which graph represents the inverse of $y = \left(\frac{1}{6}\right)^x$?

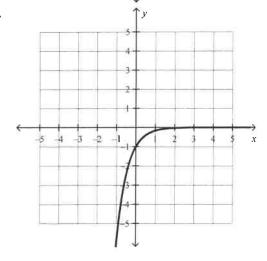
A.



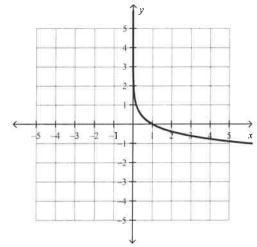
C.



B.

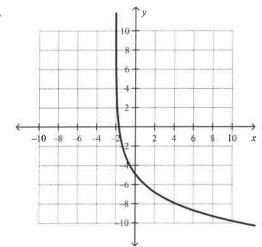


D.

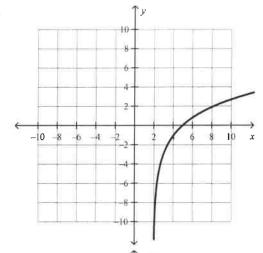


2. Which graph represents the function $y = -3 \log_3[(x-2)] - 3$?

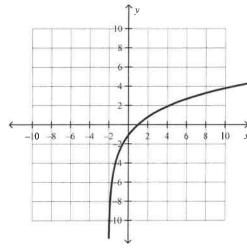
A.



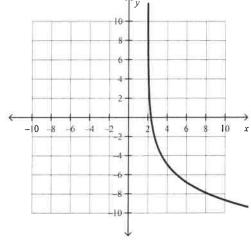
C.



B.

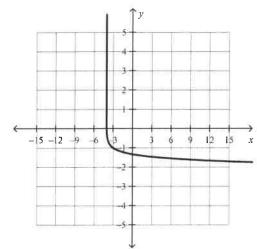


D.

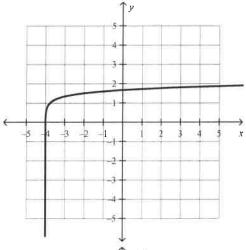


3. Which graph represents the function $y = \frac{1}{3} \log_4(x-3) + 4$?

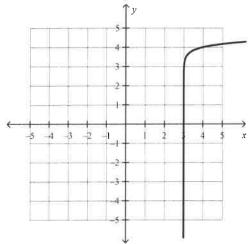
A.



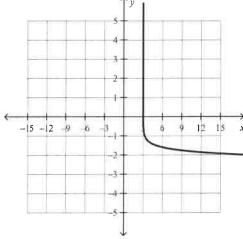
C



В.



D.



4. The domain of the function $f(x) = 8 \log_6 [8(x+8)] + 7$ is

A.
$$\{x | x < 7, x \in R\}$$

C.
$$\{x | x > 7, x \in R\}$$

B.
$$\{x | x < -8, x \in R\}$$

D.
$$\{x | x > -8, x \in R\}$$

5. What is the equation for the asymptote of the function $f(x) = -\log_7[-5(x+2)] - 3$?

A.
$$x = 2$$

C.
$$x = -5$$

B.
$$x = -3$$

D.
$$x = -2$$

Short Answer

1. Evaluate $\log_2 \sqrt[4]{32}$ without a calculator.

2. Expand the expression $\log_6 rw^2 x$ in terms of individual logarithms of the variables.

3. Simplify the expression $2 \log_2 12 - (\log_2 6 + \frac{1}{3} \log_2 27)$ without a calculator.

4. Write the expression $\log_3 r + 6 \log_3 v - \log_3 x$ as a single logarithm is simplest form.

5. Simplify $3\log\sqrt{x} + 2\log x - \frac{1}{2}\log x$

6. If $\log 3 = s$, $\log 5 = v$, and $\log 7 = z$, an algebraic expression in terms of s, v, and z for $\log \frac{5}{441}$ is

7. Given $\log_2 7 = k$ write an algebraic expression, in terms of k, for the value of $\log_2 392$.

8. Solve $\log_3 x = \log_3 2 + \log_3 3$.

9. Solve the equation $\log_2 \sqrt{x^2 - 8x} = \log_2 3$.

10. Solve the equation $\log \sqrt[3]{x^2 + 48x} = \frac{2}{3}$

11. Solve $\log(3x+15) = 1 + \log(x+3)$.

12. Solve $2 \log_4(x+4) - \log_4(x+12) = 1$

13. Solve $1500 = 5e^{0.045x}$ to the nearest thousandth.

14. Solve $9^{3x-10} = 8^{x+6}$. Round your answer to two decimal places.

15. Solve $13(5)^{4x-3} = 8^{2x+5}$, Round your answer to 2 decimal places.

16. Suppose that the population of a small town doubles every 25 years. How long does it take to triple, to the nearest tenth of a year?

17. The eye size of many vertebrates is related to body mass by the logarithmic equation $\log E = \log 10.61 + 0.1964 \log m$, where E is the eye axial length, in millimetres, and m is the body mass, in kilograms. Predict the mass of a vertebrate with an eye axial length of 43 mm. Round your answer to the nearest hundredth of a kilogram.

18. A 200-g sample of a radioactive substance is placed in a chamber to be tested. After 3 h, 140 g of the sample remains. Determine the half-life of this substance, to the nearest hundredth of an hour.

19. For his dream car, Bruce invested \$18 000 at 7.8% interest per annum, compounded semi-annually. How long will he have to invest in order to have a total of \$35 000? Round to the nearest tenth of a year.

20. In 1997, the population of a city was 795 000. This was an increase of 3.06% from the previous year. Assuming that the population is growing continuously, to the nearest tenth of a year, how long it take for the population to exceed 1 million?

Pre-Calculus 12 Chapter 8 Review

Answer Section

MULTIPLE CHOICE

- ANS: D PTS: 1 DIF: Easy OBJ: Section 8.1 NAT: RF7 TOP: Understanding Logarithms KEY: graph | inverse
 ANS: D PTS: 1 DIF: Average OBJ: Section 8.2 NAT: RF8 TOP: Transformations of Logarithmic Functions KEY: horizontal translation | vertical translation | vertical stretch | horizontal stretch
- 3. ANS: B PTS: 1 DIF: Average OBJ: Section 8.2
 - NAT: RF8 TOP: Transformations of Logarithmic Functions KEY: horizontal translation | vertical translation | vertical stretch
- 4. ANS: D PTS: 1 DIF: Average OBJ: Section 8.2
- NAT: RF8

 TOP: Transformations of Logarithmic Functions
 - KEY: domain | logarithmic functions
- 5. ANS: D PTS: 1 DIF: Average OBJ: Section 8.2
 - NAT: RF8 TOP: Transformations of Logarithmic Functions

KEY: horizontal translation | asymptote

SHORT ANSWER

1. ANS:

 $\frac{5}{4}$

- PTS: 1 DIF: Average OBJ: Section 8.1 NAT: RF7
 TOP: Understanding Logarithms KEY: logarithm NOT: Draft
- **2.** ANS:

 $\log_6 r + 2\log_6 w + \log_6 x$

- PTS: 1 DIF: Easy OBJ: Section 8.3 NAT: RF9
 TOP: Laws of Logarithms KEY: product law | laws of logarithms
- **3.** ANS:

3

PTS: 1 DIF: Easy OBJ: Section 8.3 NAT: RF9

TOP: Laws of Logarithms | KEY: product law | laws of logarithms | quotient law

4. ANS:

 $\log_3 \frac{rv^6}{x}$

PTS: 1 DIF: Easy OBJ: Section 8.3 NAT: RF9
TOP: Laws of Logarithms KEY: product law | laws of logarithms

5. ANS:

 $3 \log x$

PTS: 1

DIF: Average

OBJ: Section 8.3 NAT: RF9

TOP: Laws of Logarithms

KEY: laws of logarithms | power law | quotient law | product law

6. ANS:

v - 2s - 2z or v - (2s + 2z) or v - 2(s + z)

PTS: 1

DIF: Average

OBJ: Section 8.3 NAT: RF9

TOP: Laws of Logarithms

KEY: product law | laws of logarithms | quotient law

7. ANS:

2k + 3

PTS: 1

DIF: Difficult

OBJ: Section 8.3

NAT: RF9

TOP: Laws of Logarithms

KEY: power law of logarithms

8. ANS:

x = 6

PTS: 1

DIF: Average

OBJ: Section 8.4

NAT: RF10

TOP: Logarithmic and Exponential Equations

KEY: logarithmic equation

9. ANS:

$$x = 9 \text{ or } x = -1$$

Check the values for extraneous roots.

In this case, both values are possible.

PTS: 1

DIF: Difficult

OBJ: Section 8.4 NAT: RF10

TOP: Logarithmic and Exponential Equations

KEY: logarithmic equation | extraneous roots

10. ANS:

$$x = -50 \text{ or } x = 2$$

Check the values for extraneous roots.

In this case, both solutions are possible.

PTS: 1

DIF: Difficult

OBJ: Section 8.4 NAT: RF10

TOP: Logarithmic and Exponential Equations

KEY: logarithmic equation | extraneous roots

11. ANS:

$$-\frac{15}{7}$$

PTS: 1

DIF: Average

OBJ: Section 8.4

NAT: RF10

TOP: Logarithmic and Exponential Equations

KEY: logarithmic equation

x = -8, x = 4Since x = -8 is an extraneous root, the solution is x = 4. DIF: Average OBJ: Section 8.4 NAT: RF10 TOP: Logarithmic and Exponential Equations KEY: logarithmic equation | laws of logarithms NOT: Draft 13. ANS: 126,751 PTS: 1 DIF: Easy OBJ: Section 8.4 NAT: RF10 TOP: Logarithmic and Exponential Equations KEY: exponential equation 14. ANS: 7.63 PTS: 1 DIF: Average OBJ: Section 8.4 NAT: RF10 TOP: Logarithmic and Exponential Equations KEY: logarithmic equation | exponential equation **15.** ANS: 5.56 PTS: 1 16. ANS: It will take 39.6 years for the population to triple. PTS: 1 DIF: Difficult + OBJ: Section 8.3 | Section 8.4 NAT: RF9 TOP: Laws of Logarithms | Logarithmic and Exponential Equations KEY: power law | law of logarithms | logarithmic equation | exponential equation 17. ANS: 1242.98 **PTS**: 1 DIF: Difficult OBJ: Section 8.1 | Section 8.4 NAT: RF10 | RF7 TOP: Understanding Logarithms | Logarithmic and Exponential Equations KEY: exponential equation | logarithmic equation **18.** ANS: The half-life is 5.83 h. DIF: Difficult OBJ: Section 8.4 NAT: RF10 TOP: Logarithmic and Exponential Equations KEY: exponential equation | logarithmic equation Bruce will need invest for approximately 8.7 years. DIF: Difficult PTS: 1 OBJ: Section 8.4 NAT: RF10 TOP: Exponential and Logarithmic Equations KEY: exponential function | logarithmic equation 20. 7.5 years

12. ANS: